## Research Article

## Advances in Theoretical \& Computational Physics

# The Proton, Gravity, and Black Hole Equations 

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#### Abstract

In these papers, I presented and explained the Potential Energy Equation "P.E.E."; this equation is about discovering how gravitation works, the cosmological facts for the Black Hole physics "B.H.", and the "B.H." primary role in the gravitational energy at both the astronomical (planets: Earth, Sun, etc.) and microscopic atomic (Protons) levels. "P.E.E." equation is uncovering a new concept for the Planck Constant and the Fine Structure, as an inhibition for the "B.H." energy and as a convertor from one type of energy to another in the "P.E.E." energies parts; this new concept is also explaining the "Attractive Mass" or "central mass" and redefining the Gravitational Potential Energy $U_{g}$; and the Kinetic Energy as well; and it is clarifying the difference in apply between $U_{g}$ and the Weak Potential Energy of mass (Attracted Mass) " $A_{g}$ ". I already defined the "B.H." potential energy ( $f$ ) equation, the mass compressed " $N_{p}$ " with radius" $r_{s}$ " of the "B.H" equation, the mass compressing distance " $r_{c}$ " and the radius " $r$ " of the "B.H." equation; and the gravitational and "B.H." energy equations; I have also applied these equations on astronomical and microscopic dimensions.


Keywords: Gravitation, Black hole, Sun, Proton

In these papers, we will attempt to comprehend the gravitational potential energy in large astronomical mass levels, such as planets, based on the extremely tiny microscopic mass levels, such as atoms. This will unify the physical sciences.The identical mathematical structure of the Newton gravitation law and the Coulomb charge law inspires the notion that there is a relationship between them, which is the $\left(f_{s}\right)$ or what we will conclude later is the "B.H." potential energy component; these three energy components constitute the "P.E.E." equation.From the calculation of the frequency $\left(\boldsymbol{f}_{\boldsymbol{s}}\right)$ formula in terms of the speed of light and the distance between the charges or masses (equation 5), I determined that the $\left(\boldsymbol{f}_{s}\right)$ value is equal to the potential electromagnetic energy value between these charges or masses, indicating that ( $\boldsymbol{h}^{\mathbf{0}}=\mathbf{1}$ ). In addition, I formulated the "P.E.E." equation using the Planck and Fine structure constants. According to the "P.E.E." equation's results, in its formula of Planck and Fine structure constants, there is no direct equivalence between the weak potential energy of mass " $\boldsymbol{A}_{g}$ " and K.E at the microscopic atomic level; instead, we must add a mathematical change in the " $\boldsymbol{A}_{g}$ " to obtain " $\boldsymbol{U}_{g}$ ", whose value is equal to direct K.E; this change creates a new concept, the "Attractive Mass."

I concluded by defining the "B.H." equations and explicating their relationship to the "Attractive Mass" via the "B.H." $\left(r_{s}\right)$. I concluded by describing and supplying the equations for the "B.H." black hole.In addition, I discussed significant examples of calculations that apply to the new K.E. equation at the
microscopic atomic and large astronomical body levels.In addition, I applied the new equations for gravity and "B.H." to the microscopic atomic and large astronomical bodies level and calculated the acceleration of the Earth's gravity (g).

## 2. The Potential Energy Equations "P.E.E." and "B.H."

The "P.E.E." defines the "B.H." potential energy by its hidden protons mass-weak potential energy (Attracted Mass) $\left(A_{g}\right)$ and its hidden charges potential energy $\left(U_{g}\right)$; and I say hidden because the protons and charges are contained within the "В.Н.". The equation reveals that the $\left(6 . f_{s}\right)$ where $\left(f_{s}\right)$ "B.H." potential energy or frequency value at the same time (I will elaborate on this point in Section 4); and is compressing by distance ( $r_{c}$ ) inside this "B.H."; and multiplied the weak potential energy of the hidden proton square mass (Attracted Mass) $\left(A_{g}\right)$ and is also compressing by distance $\left(r_{c}\right)$ inside this "B.H." This leads to the square of the hidden charge's potential energy $\left(U_{q}^{2}\right)$, of these protons. This system of hidden protons, masses, and "B.H." can constitute the "Attractive Mass" or "central mass." This mass's hidden contents have an effect on masses that aren't hidden or located outside of the "B.H.", such as charged masses like the proton or neutral masses like the neutron, or ionized or neutral atoms. Fundamental to the definitions of "Attractive Mass" and "B.H." is the availability of potential energy between these concealed charges, not the sum of these electrical charges. The primary function of "B.H." or "Attractive Mass" is to position each unhidden charge or mass in a specific orbit where there is
neither infinite repulsion if the charges are similar nor fusion if the charges are dissimilar; in other words, the availability of "B.H." energy is what creates stability.

The "P.E.E." formula:

$$
\begin{align*}
& \text { 6. } f_{s} \cdot A_{g}=U_{q}^{2}  \tag{1}\\
& \text { 6. } \frac{c}{2 \pi r_{c}} \cdot G \frac{m_{p 1} \cdot m_{p 2}}{r_{c}}=\left(\frac{1}{4 \pi \epsilon_{0}} \cdot \frac{q_{1} \cdot q_{2}}{r_{c}}\right)^{2} \tag{1}
\end{align*}
$$

The "P.E.E." element in the " $m$ " and " c " equation (3) can be expressed as the Einstein mass-energy equivalent equation [1], where this energy equals the compressing energy imparted by "B.H.":

$$
\begin{equation*}
\text { 6. } \frac{c}{2 \pi r_{c}} \cdot G \frac{m_{p 1} \cdot m_{p 2}}{r_{c}}=\left(m \cdot c^{2}\right)^{2} \tag{2}
\end{equation*}
$$

Where:

$$
\begin{equation*}
U_{q}=\frac{1}{4 \pi \epsilon_{0}} \frac{q_{1} \cdot q_{2}}{r_{c}} \tag{3}
\end{equation*}
$$

$U_{q}$ : represents the charge potential energy in joules [2] .
$q_{1}, q_{2}$ : are the charges, and each one corresponds to the electron charge of $1.67 \times 10^{-19}$ coulombs [3].
$\epsilon_{0}$ : represents the vacuum permittivity, which is $8.85 \times 10^{-12}$ f.m ${ }^{-1}$ ) [4].
$r_{c}$ : is the separation between the two charges (or the compressing distance for protons within "B.H.").

$$
\begin{equation*}
A_{g}=G \frac{m_{p 1} \cdot m_{p 2}}{r_{c}} \tag{4}
\end{equation*}
$$

$A_{g}$ : the weak potential energy of mass (because in $A_{g}$ we use $m_{p 1}^{g}$ as a "Attracted Mass", and later we will define $U_{g}$ as gravitational potential energy because in $U_{g}$ relations we use $m_{p 1}$ as a "Attractive Mass".
$m_{p 1}$ and $m_{p 2}$ are the proton masses $1.67 \times 10^{-27} \mathrm{~kg}$ [5]
$\mathrm{G}^{p 1}$ is the gravitational constant $6.67 \times 10^{-11}\left(\mathrm{~m}^{3} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~s}^{-2}\right)[6]$

$$
\begin{equation*}
f_{s}=\frac{C}{2 \pi r_{c}} \tag{5}
\end{equation*}
$$

$f_{s}$ : represents the "B.H." potential energy and frequency in Hertz, where $f_{s}$. $h^{0}=f_{s}$ (I will elaborate on this point in Section 4).
$r_{c}$ : denotes both the distance between two protons and the compression distance in meter (m).
$C$ : The constant speed of light is $3 \times 10^{8} \mathrm{~m} / \mathrm{s}$ [7].
$m$ : represents the total mass-energy equivalent [8] divided by the total compressing energy from "B.H."
2.1. The applicability of the "P.E.E." to various " $r_{c}$ " and "B.H." proton examples:
The "P.E.E." is applicable to any compression distance " $r_{c}$ " within the "B.H."; therefore, if we have:
$r_{c}=1.0 \times 10^{-11} \mathrm{~m}$
Derived from equation (4): $\mathrm{U}_{\mathrm{q}}{ }^{2}=5.3 \times 10^{-34} \mathrm{~J}^{2}$,
Derived from equation (6): $f_{s}=4.7770 \times 10^{18} \mathrm{~J}$,
Derived from equation (5): $\quad A_{g}=1.86 \times 10^{-53} \mathrm{~J}$
So:

$$
\left(6 . f_{s} \cdot A_{g}\right) / U_{q}^{2}=1.005888
$$

We will repeat what was done above:

$$
\text { For: } r_{c}=1.0 \times 10^{-7} \mathrm{~m}
$$

$$
U_{q}^{2}=5.3 \times 10^{-42} \mathrm{~J}^{2}
$$

$$
f_{s}=4.777 \times 10^{14} \mathrm{~J}
$$

$$
A_{g}=1.86 \times 10^{-57} \mathrm{~J}
$$

Therefore:

$$
\begin{aligned}
& \left(6 . f_{s} \cdot A_{g}\right) / U_{q}^{2}=1.005888 \\
& \text { For } r_{c}=1.0 \times 10^{-4} \mathrm{~m} \\
& U_{q}^{2}=5.3 \times 10^{-48} \mathrm{~J}^{2} \\
& f_{s}=4.777 \times 10^{11} \mathrm{~J} \\
& A_{g}=1.86 \times 10^{-60} \mathrm{~J}
\end{aligned}
$$

Therefore:

$$
\left(6 . f_{s} \cdot A_{g}\right) / U_{q}^{2}=1.005888
$$

By substituting the previously calculated values into the "P.E.E." formula, we find that the percentage ratio for both sides is (1.005888); therefore, both sides of the formula are equal.

### 2.1.1. The "B.H." of the Proton example

where the neutron is not as stable as the proton (its mean lifetime is 879.4 (6) s [9]; I will use the proton as an example for the validity of the "P.E.E."

For a single proton, we'll use the following equation (3):
Here, the (mass-energy equivalent) ( m ) should equal total Proton mass( m_(p )), therefore:

$$
U_{q}=m_{p} \cdot c^{2}=1.5 \times 10^{-10} \mathrm{~J}
$$

Derived from equation (14)

$$
f_{s}=\frac{U_{q}}{\alpha . h}=3.107 \times 10^{25} \mathrm{~J}
$$

Derived from equation (6)

$$
r_{c}=\frac{c}{2 \pi . f_{s}}=1.5 \times 10^{-18} \mathrm{~m} \text {, (the compressing distance) }
$$

(Note: I have already resolved this example in Section 12 using the equation (36), which contains the number of hidden Protons $\left(N_{p}\right)$; and I obtained the same value for " $r_{c}$ ")

So:

$$
\begin{aligned}
& U_{q}^{2}=2.35 \times 10^{-20} \mathrm{~J}^{2}, f_{s}=3.107 \times 10^{25} \mathrm{~J} \\
& A_{g}=1.24 \times 10^{-46} \mathrm{~J}
\end{aligned}
$$

And if we substitute these values into the "P.E.E." formula, we find that the percentage ratios for both sides are:

$$
\left(6 . f_{s} \cdot A_{g}\right) / U_{q}^{2}=0.98366
$$

Therefore, both sides are equal.
3. P.E.E. Derived

From the previous, we know that:

$$
A_{g}=G \frac{m_{p 1} \cdot m_{p 2}}{r_{c}}, \quad U_{q}=\frac{1}{4 \pi \epsilon_{0}} \frac{q_{1} \cdot q_{2}}{r_{c}}
$$

We can express $U_{q}$ in terms of the charges of the electric field (E) and the storage volume (V) [10]:

$$
\begin{equation*}
U_{q}=\epsilon_{0} \cdot E^{2} . V \tag{6}
\end{equation*}
$$

So:

$$
\begin{align*}
& U_{q}^{2}=\epsilon_{0}{ }^{2} \cdot E^{4} \cdot V^{2}  \tag{7}\\
& \frac{U_{q}^{2}}{A_{g}}=\frac{\epsilon_{0}^{2} \cdot E^{4} \cdot V^{2} \cdot r_{c}}{G \cdot m_{p}^{2}} \tag{8}
\end{align*}
$$

Where $m_{p 1}=m_{p 2}=m_{p}$ and $r_{c}=r$
and if

$$
\begin{align*}
& m_{p} \cdot v^{2}=\epsilon_{0} \cdot E^{2} \cdot V  \tag{9}\\
& \frac{U_{q}^{2}}{A_{g}}=\frac{\epsilon_{0}^{2} \cdot v^{4} \cdot V^{2} \cdot r}{\epsilon_{0}^{2} \cdot G \cdot V^{2}} \tag{10}
\end{align*}
$$

The calculation revealed, however, that the right side must be multiplied by the fraction (1/6) for the uber relation to be valid, so:

$$
\begin{equation*}
\frac{U_{q}{ }^{2}}{6 . A_{g}}=\frac{v^{4} \cdot r}{G}=f_{s} \tag{11}
\end{equation*}
$$

(I will explain later that " $r$ " here corresponds to the "B.H." radius " $r$ "; $v=c$ and " $r_{d}$ " utilizing $U_{g}$ )

## 4. The "B.H" $\left(f_{s}\right)$ Energy Units

I've already mentioned that the $f_{s}$ value can be viewed as a frequency and an energy at the same time, Below is the derivation
of its unit:
based on the conclusion reached in Section 3:

$$
f_{s}=\frac{v^{4} \cdot \mathrm{r}}{G} \quad \text { is } \quad\left(\frac{m^{4} \cdot \mathrm{~m}}{\mathrm{~s}^{4}} \cdot \frac{\mathrm{~kg} \cdot \mathrm{~s}^{2}}{\mathrm{~m}^{3}}=\frac{\mathrm{kg} \cdot \mathrm{~m}^{2}}{\mathrm{~s}^{2}}=\text { Joule }\right)
$$

The calculation also revealed the following relationship between $c, r_{c}$ and $f_{s}$ :

$$
f_{s}=\frac{c}{2 \pi r_{c}} \text { is } \quad\left(\frac{m}{s . m}=\operatorname{Hertz}\right)
$$

## 5. Planck Constant and P.E.E.

The charge potential energy can be expressed as follows in terms of the magnetic wave frequency, blank constant, and fine structure constant:

$$
\begin{equation*}
U_{q}=\alpha . h . f \tag{12}
\end{equation*}
$$

Where:
$h$ : represents the Planck constant, $6.626 \times 10^{-34} \mathrm{~J} . \mathrm{Hz}^{-1}[11]$
$\square$ : is the constant of fine structure $\frac{1}{137} \quad$ [12]
And if we assume that $f=f_{s}$
then

$$
\begin{equation*}
U_{q}=\alpha \cdot h \cdot f_{s}, \tag{13}
\end{equation*}
$$

Moreover,

$$
\begin{equation*}
U_{q}{ }^{2}=\alpha^{2} \cdot h^{2} \cdot f_{s}^{2} \tag{14}
\end{equation*}
$$

Based on equation (12), we can write

$$
\begin{equation*}
\text { 6. } A_{g}=\alpha^{2} \cdot h^{2} \cdot f_{s} \tag{15}
\end{equation*}
$$

Therefore, Based on equation (12) and (14), we can write

$$
\begin{equation*}
U_{q}=\frac{6 . A_{g}}{\alpha \cdot h} \tag{16}
\end{equation*}
$$

Therefore, the P.E.E. can then be written as follows:

$$
\begin{equation*}
f_{s} \cdot \alpha^{2} \cdot h^{2} \cdot f_{s}=\alpha^{2} \cdot h^{2} \cdot f_{s}^{2} \tag{17}
\end{equation*}
$$

We can equalize charge potential energy and kinetic energy in the following manner:

$$
\begin{equation*}
U_{q}=2 . K E=m_{p} \cdot v^{2} \tag{18}
\end{equation*}
$$

So:

$$
\begin{equation*}
\text { 6. } A_{g}=\text { 2. } \alpha . h . K E \tag{19}
\end{equation*}
$$

So:

$$
\begin{equation*}
\text { 3. } A_{g}=\alpha . h . K E \tag{20}
\end{equation*}
$$

From equations (14), (16), and (21), we can determine the significance of the Planck and Fine Structure Constants, in which these constants serve as an inhibition or constant converting instrument for converting from one form of energy to another; this is the new concept for the Planck constant.
6. Kinetic Energy (KE) and Gravitational Energy ( $\mathbf{U}_{\mathrm{g}}$ ) Relations
Observing from Equation (20) that there is a ratio ( $\frac{3}{\alpha . h}$ ) between the KE and the "mass potential weak energy," $A_{g}$,
and if :

$$
K E=U_{g}
$$

Therefor, we can now define the "gravitational potential energy" as follows:

$$
\begin{equation*}
U_{g}=G \frac{\frac{3 \cdot m_{p 1}}{\alpha \cdot h} \cdot m_{p 2}}{r_{d}} \tag{21}
\end{equation*}
$$

Where:
$r_{d}$ : is the distance for the mass m from the "B.H" or "Attractive Mass" central

The kinetic energy will therefore be:

$$
\begin{equation*}
K E=U_{g}=G \frac{\frac{3 \cdot m_{p}}{\alpha \cdot h} \cdot m_{p}}{r_{d}} \tag{22}
\end{equation*}
$$

The attractive and attracted bodies for N protons are calculated as follows:

$$
\begin{equation*}
K E=G \frac{\frac{3 . N_{p 1} \cdot m_{p 1}}{\alpha \cdot h} \cdot N_{p 2} \cdot m_{p 2}}{r_{d}} \tag{23}
\end{equation*}
$$

Therefor, we can now define:

$$
\begin{gather*}
M=\frac{3 \cdot N_{p 1} \cdot m_{p 1}}{\alpha \cdot h} \quad \text { (Attractive Mass) }  \tag{24}\\
m=N_{p 2} \cdot m_{p 2} \text { (Attracted Mass) } \tag{25}
\end{gather*}
$$

Then:

$$
\begin{equation*}
K E=U_{g}=G \frac{M \cdot m}{r_{d}} \tag{26}
\end{equation*}
$$

Therefore, if we have $W_{1,2}$; are the works of the gravitational force $\left(F_{g}\right)$;and $(g)$ is the acceleration of gravity; where both $\left(F_{g}\right)$ and (g) are related to the Attractive Mass $M$; where ( $r_{d 2}>r_{d 1}$ ), and $\left(r_{d 2}-r_{d 1}=r_{d}\right)$ :

$$
\begin{equation*}
W_{1}=G \frac{M \cdot m}{r_{d 1}} \tag{27}
\end{equation*}
$$

, and

$$
\begin{align*}
& W_{2}=G \frac{M \cdot m}{r_{d 2}}  \tag{28}\\
& W_{1}=F_{g} \cdot r_{d 1}=g \cdot m \cdot r_{d 1} \tag{29}
\end{align*}
$$

and;

$$
\begin{gather*}
W_{2}=F_{g} \cdot r_{d 2}=g \cdot m \cdot r_{d 2}  \tag{30}\\
K E=U_{g}=W_{2}-W_{1}=F_{g} \cdot\left(r_{d 2}-r_{d 1}\right)=F_{g} \cdot r_{d} \tag{31}
\end{gather*}
$$

## 7. The Kinetic Energy (KE) and Gravitational Energy ( $\boldsymbol{U}_{g}$ )

## Calculation Problem

We do not have a problem with astronomical bodies because we already use the "Attractive Mass" implicitly in the planet mass (big mass) "M." in equations (24) and (27) in Newton's Law to calculate $\left(U_{g}\right)$ and $(K E)$, but we do have a problem with atomic microscopy level; when we apply the "weak mass potential energy" $\left(A_{g}\right)$ or equation :

$$
A_{g}=G \frac{m_{p 1} \cdot m_{p 2}}{r_{d}}
$$

and consider it as $\left(U_{g}\right)$ and $(K E)$. In reality, when we use this (Attracted Mass) I mean (the value of $m_{p}$ only) in our calculations, the values for $\left(A_{g}\right)$ will not represent the true attractive energies (very weak energy), and we cannot rely on these atomic energy values to determine the energy of a large body (complex body). Multiplying $\left(U_{g}\right)$ and $(K E)$ for a single proton by $\left(N_{p}\right)$, the number of protons for both masses, is all that is required. Using its attractive mass $M$, I will illustrate how to solve the problem below.

### 7.1. Level of Atomic Microscopy

The "Weak mass potential energy" for two protons with $r_{d}=$ $1.0 \times 10^{-4} \mathrm{~m}$ when we are using the (Attracted Mass):

$$
A_{g}=G \frac{m_{p}^{2}}{r_{d}}=\frac{\left(6.67 \times 10^{-11}\right)\left(1.67 \times 10^{-27}\right)^{2}}{\left(1.0 \times 10^{-4}\right)}=1.86 \times 10^{-60} \mathrm{j}
$$

The gravitational potential energy for two protons with $r_{d}=$ $1.0 \times 10^{-4} \mathrm{~m}$; when we are using the (Attractive Mass):
$U_{g}=G \frac{\frac{3 . m_{p 1}}{\alpha . h} \cdot m_{p 2}}{r_{d}}=\frac{\left(6.67 \times 10^{-11}\right) \cdot \frac{3 \cdot\left(1.67 \times 10^{-27}\right)}{\left(\frac{1}{137}\right) \cdot\left(6.626 \times 10^{-34}\right)} \cdot\left(1.67 \times 10^{-27}\right)}{\left(1.0 \times 10^{-4}\right)}=3.85 \times 10^{-25} \mathrm{j}$
The last example demonstrates that the $\left(A_{\mathrm{g}}\right)$ formula yielded a very weak energy value, whereas the $\left(U_{g}\right)$ formula yielded the potential energy value, which is sufficient to provide thermal energy and motion for molecules $\left(1.0 \times 10^{-4} \mathrm{~m}\right.$, it is in the infrared spectrum of electromagnetic radiation [13].

### 7.2. Level of astronomical bodies:

We will now apply the last equation to the large bodies: the Earth, mass, and $r_{d}$ (the Earth' s radius) $=1 \mathrm{~kg} 6.36 \times 10^{6} \mathrm{~m}$ [14]:
The (Attractive Mass) for Earth $=M=5.9 \times 10^{24} \mathrm{~kg}$

$$
\text { so according to } M=\frac{3 \cdot N_{p 1} \cdot m_{p}}{\alpha \cdot h}
$$

$N_{p 1}$ (number of proton in Earth "B.H" ) $=5.69 \times 10^{15}$ protons. (In sections 8 and 9 , I will explain how and why this number, " $N_{p}$ " was derived)

And for the mass:

$$
\begin{aligned}
& N_{p 2}(\text { number of proton in the mass })=\frac{1 \mathrm{~kg}}{m_{p}}=5.98 \times 10^{26} \text { protons } \\
& U_{g}=G \frac{\frac{3 . N_{p 1} \cdot m_{p}}{\alpha . h} \cdot N_{p 2} \cdot m_{p}}{r_{d}}=\frac{\left(6.67 \times 10^{-11}\right) \cdot \frac{3 \cdot\left(5.69 \times 10^{15}\right) \cdot\left(1.67 \times 10^{-27}\right)}{\left(\frac{1}{137}\right) \cdot\left(6.626 \times 10^{-34}\right)} \cdot\left(5.98 \times 10^{26}\right) \cdot\left(1.67 \times 10^{-27}\right)}{\left(6.36 \times 10^{6}\right)} \\
& =6.1 \times 10^{7} \mathrm{j} \\
& U_{g}=2 . K E=m . v^{2}
\end{aligned}
$$

Where $m=N_{p 2} \cdot m_{p}$
So,

$$
v^{2}=\frac{2\left(6.1 \times 10^{7}\right)}{1 . \mathrm{kg}}
$$

and

$$
v=11.1 \times 10^{3} \mathrm{~ms}^{-1}
$$

## 8. The Attractive Mass and the Black Hole

We have already discussed "Attractive Mass" in equation (25):

$$
M=\frac{3 \cdot N_{p 1} \cdot m_{p}}{\alpha \cdot h}(\text { the Attractive Mass })
$$

Consequently, this is the mass calculation approach that must always be used when $\left(A_{g}\right)$ must equal KE based on our equation (21):

$$
\text { 3. } A_{g}=\alpha \cdot h \cdot K E
$$

This is the mass that we already always use in our calculations when dealing with the gravitational force of large bodies (complex bodies) such as planets (Sun, Earth, etc.)

$$
\begin{equation*}
K E=G \frac{M \cdot m}{r_{d}} \tag{32}
\end{equation*}
$$

I have already clarified the relationship between this " Attractive Mass " and the proton ( $m_{p}$ ) using $N_{p}, h$ and $\alpha$. this relationship is significant because it is the gateway between the small particle level (atoms) and the large body level, or, in other words, the connecting ring between classical and modern physics.
8.1. calculation of Earth Attractive Mass and $\left(\mathrm{N}_{\mathrm{p}}\right)$
$M=M_{\text {Earth }}=\left(5.9 \times 10^{24}\right)=\frac{3 . N_{p 1} \cdot m_{p}}{\alpha . h}=\frac{3 \cdot N_{\mathrm{p} 1} .\left(1.67 \times 10^{-27}\right)}{\left(\frac{1}{137}\right)\left(6.626 \times 10^{-34}\right)}$
$\mathrm{N}_{\mathrm{p} 1}($ number of protons in the Earth's black hole $)=5.69 \times 10^{15}$ protons

The $\left(N_{p}\right)$ calculation reveals that the Earth's Attractive Mass derives its effect not only from the number of $\operatorname{masses}\left(N_{p} \cdot m_{p}\right)$, but also from the compression of this mass as a result of its availability in its black hole; see Section 10.

## 9. The derivative relationships of the "B.H."

From equations (21) and (24), we know:
3. $A_{g}=\alpha \cdot h . K E$
$K E=G \frac{\frac{3 \cdot N_{p 1} \cdot m_{p 1}}{\alpha \cdot h} \cdot N_{p 2} \cdot m_{p 2}}{r_{d}}$

Therefore:

$$
\begin{equation*}
G \frac{3 \cdot N_{p} \cdot m_{p} \cdot N_{p} \cdot m_{p}}{r_{d}}=\alpha \cdot h \cdot \frac{1}{2} \cdot N_{p} \cdot m_{p} \cdot v^{2} \tag{33}
\end{equation*}
$$

For inside the "B.H" $v^{2}=C^{2}$ and $r_{d}=r_{s}$;
Consequently,

$$
\begin{equation*}
G \frac{6 \cdot \frac{N_{p} \cdot m_{p}}{\alpha . h}}{r_{s}}=C^{2} \tag{34}
\end{equation*}
$$

; Therefore,

$$
\begin{equation*}
\frac{N_{p}}{r_{s}}=\frac{C^{2} \cdot \alpha . h}{6 . G . . m_{p}} \tag{35}
\end{equation*}
$$

$$
\frac{6 \cdot N_{p} \cdot m_{p}}{\alpha \cdot h}=\frac{C^{2} \cdot r_{S}}{G}
$$

And using the following equation (24):

$$
\begin{equation*}
2 . M=\frac{C^{2} \cdot r_{S}}{G} \tag{36}
\end{equation*}
$$

Already in 1916, the German astronomer Karl Schwarzschild obtained the exact solution to Einstein's field equations [15] for the gravitational field outside a non-rotating, spherically symmetric body with mass and discovered the same relation (37), but I used the "P.E.E." equation and the "Attractive Mass" concept here.

Where:
M:represents the "Attractive Mass" in kilograms
$r_{s}:$ represents the "B.H" radius in meter
$C$ : the constant of light speed
$N_{p}$ : the number of compressed protons inside the "B.H."
Equations (25), (37) demonstrate that the "Attractive Mass" M increases as the number of compressed protons $N_{p}$ inside the "B.H." and the radius of the "B.H." both increases.
10. Derivation of P.E.E. and black hole relationships

The final equation (6) states:

$$
f_{s}=\frac{C}{2 \pi r_{c}}
$$

$r_{c}$ : is the distance between protons within the "B.H." (or the compressing distance for protons within the "B.H."). And according to the final equation (10):

$$
f_{s}=\frac{v^{4} \cdot r_{d}}{G}
$$

Moreover, if $v=C$ and $r_{d}=r_{s}$ so:

$$
\begin{equation*}
f_{S}=\frac{c^{4} \cdot r_{s}}{G} \tag{37}
\end{equation*}
$$

$r_{s}$ : represents the "B.H" radius in meter
Equation (38) demonstrates that the "B.H." energy (or frequency, as previously explained in Section 4) increases as the "B.H." radius increases, as does its energy.

And using equations (5) and (38), we can formulate the following:

$$
\begin{equation*}
\frac{c}{2 \pi r_{c}}=\frac{c^{4} \cdot r_{S}}{G} \tag{38}
\end{equation*}
$$

Then:

$$
\begin{equation*}
r_{S} \cdot r_{c}=\frac{G}{2 \pi . c^{3}} \tag{39}
\end{equation*}
$$

It is evident from Equations (38) and (40) that there is an inverse relationship between " $r_{s}$ " and " $r_{c}$," such that if the "B.H." compresses its contents more (the " $r_{c}$ " decreases), then its radius, or energy for compressing, or gravity will increase.

From (37) and (40), we can deduce the following:

$$
\begin{gather*}
2 M=\frac{c^{2}}{G} \cdot \frac{G}{2 \pi \cdot c^{3} \cdot r_{c}}=\frac{1}{2 \pi \cdot c \cdot r_{c}}  \tag{40}\\
M=\frac{1}{4 \pi \cdot c \cdot r_{c}} \tag{41}
\end{gather*}
$$

Equation (42) demonstrates that the "Attractive Mass" $M$ increases as the compressing distance " $r_{c}$ " for protons within "B.H." shrinks.

We are aware of the P.E.E. formula:

$$
\text { 6. } \frac{C}{2 \pi r_{c}} \cdot \quad G \frac{m_{p 1 .}^{2} \cdot m_{p 2}^{2}}{r_{c}}=\left(\frac{1}{4 \pi \epsilon_{0}} \cdot \frac{q_{1} \cdot q_{2}}{r_{c}}\right)^{2}
$$

Therefore, we can now express the P.E.E. equation as follows:

$$
\begin{equation*}
\text { 6. } \frac{c^{4} \cdot r_{S}}{G} \cdot \quad G \frac{m_{p 1}^{2} \cdot m_{p 2}^{2}}{r_{c}}=\left(\frac{1}{4 \pi \epsilon_{0}} \cdot \frac{q_{1} \cdot q_{2}}{r_{c}}\right)^{2} \tag{42}
\end{equation*}
$$

Or

$$
\text { 6. } \frac{c^{4} \cdot r_{s}}{G} . \quad A_{g}=U_{q}^{2}
$$

When the distance between the charges (or the compressing distance for protons inside "B.H.") $\left(r_{c}\right)$ increases, it is evident that the square charge $\left(\mathrm{U}_{\mathrm{q}}{ }^{2}\right)$ potential and the mass potential weak energy $\left(A_{g}\right)$ decrease; simultaneously, the $\left(r_{s}\right)$ decreases and the "B.H." energy decreases.
11. The Earth and Sun Calculation of the "B.H." radius ( $r_{s}$ ) and its compressing distance ( $r_{c}$ )

### 11.1. Earth

We know from last calculation that the
$N_{p}($ for Earth $)=5.69 \times 10^{15}$ protons, and according to the equation (36), therefor:

$$
\begin{aligned}
& \frac{N_{p}}{r_{s}}=\frac{C^{2} \cdot \alpha \cdot h}{6 . G . m_{p}} \\
& \frac{1}{r_{s}}=\frac{\left(3 \times 10^{8}\right)^{2} \cdot\left(\frac{1}{137}\right) \cdot\left(6.626 \times 10^{-34}\right)}{6\left(6.67 \times 10^{-11}\right)\left(1.67 \times 10^{-27}\right) \cdot\left(5.69 \times 10^{15}\right)} \\
& r_{S}(\text { Earth Black Hole radius })=8.748 \mathrm{~mm}
\end{aligned}
$$

Using equation (40), we can also calculate the compressing distance within the "B.H."

$$
r_{c}=\frac{G}{2 \pi \cdot c^{3} r_{s}}=\frac{\left(6.67 \times 10^{-11}\right)}{2 \pi .\left(3 \times 10^{8}\right)^{3}\left(8.748 \times 10^{-3}\right)}
$$

$r_{c}($ Earth "B.H" comressing distance $)=4.49 \times 10^{-35} \mathrm{~m}$
11.2. Sun

The mass of Sun is $1.989 \times 10^{30} \mathrm{~kg}$,
And according to the final equation (37)

$$
r_{s}=\frac{2 . G . M}{C^{2}}=\frac{2 \cdot\left(6.67 \times 10^{-11}\right) \cdot\left(1.989 \times 10^{30}\right)}{2 \pi \cdot\left(3 \times 10^{8}\right)^{2}}=2.948 \times 10^{3} \mathrm{~m}
$$

$r_{s}($ Sun Black Hole radius $)=2.948 \mathrm{~km}$
$r_{c}=\frac{G}{2 \pi \cdot c^{3} r_{s}}=\frac{\left(6.67 \times 10^{-11}\right)}{2 \pi .\left(3 \times 10^{8}\right)^{3}\left(2.948 \times 10^{3}\right)}=1.33 \times 10^{-40} \mathrm{~m}$
$r_{s}($ Sun Black Hole comressing distance $)=1.33 \times 10^{-40} \mathrm{~m}$
12. Calculation of the hydrogen atom's "B.H." radius ( $r_{s}$ ) and its compressing distance ( $\mathrm{r}_{\mathrm{c}}$ )
In this instance, the Np value for the hydrogen atom is:
$\mathrm{Np}($ Hydrogen atom $)=1$ proton, and according to the equation (36), therefor:

$$
\begin{aligned}
& \frac{N_{p}}{r_{s}}=\frac{C^{2} \cdot \alpha \cdot h}{6 \cdot G . m_{p}}= \\
& \frac{1}{r_{s}}=\frac{\left(3 \times 10^{8}\right)^{2} \cdot\left(\frac{1}{137}\right) \cdot\left(6.626 \times 10^{-34}\right)}{6\left(6.67 \times 10^{-11}\right)\left(1.67 \times 10^{-27}\right) \cdot(1)}
\end{aligned}
$$

$r_{s}($ Hydrogen atom "B.H" rdius $)=1.535 \times 10^{-18} \mathrm{~m}$
Also, we can calculate the proton radius from the center of the black hole, given that there is only one proton and compression occurs on the proton itself.

$$
\begin{aligned}
& r_{c}=\frac{G}{2 \pi \cdot c^{3} r_{s}}=\frac{\left(6.67 \times 10^{-11}\right)}{2 \pi .\left(3 \times 10^{8}\right)^{3}\left(1.535 \times 10^{-18}\right)} \\
& r_{c}=2.56 \times 10^{-19} \mathrm{~m}
\end{aligned}
$$

13. Equations for gravitational and "B.H." potential energy (Gravitational Potential Energy and the "B.H" " $r_{s}$ " equation)

$$
\begin{equation*}
U_{g}=\frac{r_{s} \cdot N_{p 2} \cdot m_{p 2} \cdot C^{2}}{2 \cdot r_{d}} \tag{44}
\end{equation*}
$$

(Gravitational Force and the "B.H" " $r_{s}$ " equation)

$$
\begin{equation*}
F_{g}=\frac{r_{s} \cdot m \cdot C^{2}}{2 \cdot r_{d}^{2}} \tag{45}
\end{equation*}
$$

Where: $m=N_{p 2} . m_{p 2}$
(Gravitational Acceleration and the "B.H" " $r_{s}$ " equation)

$$
\begin{equation*}
g=\frac{r_{s} \cdot C^{2}}{2 \cdot r_{d}^{2}} \tag{46}
\end{equation*}
$$

Where:
$r_{d}$ : is the distance for the mass m from the "B.H" or "Attractive Mass" central
$F_{g}$ :is the gravity force on the mass $m$
$g$ :is the gravitation acceleration Also, from (42) we can write the gravitational potential energy in (24):
(Gravitational Potential Energy and the "B.H" " $r_{c}$ " equation)

$$
\begin{equation*}
U_{g}=\frac{G \cdot N_{p 2} \cdot m_{p 2}}{4 \pi \cdot c \cdot r_{c} r_{d}} \tag{47}
\end{equation*}
$$

(Gravitational Force and the "B.H" "r_c " equation)

$$
\begin{equation*}
F_{g}=\frac{G . m}{4 \pi \cdot c \cdot r_{c} r_{d}^{2}} \tag{48}
\end{equation*}
$$

Where: $m=N_{p 2} \cdot m_{p 2}$
(Gravitational Acceleration and the "B.H" " $r_{c}$ " equation)

$$
\begin{equation*}
g=\frac{G}{4 \pi \cdot c . r_{c} r_{d}^{2}} \tag{49}
\end{equation*}
$$

14. Calculation of the Earth's gravitational acceleration (g) And we can calculate the gravitation acceleration (g); if we have $m=1 \mathrm{~kg}$, Earth radius $r_{d}=6.36 \times 10^{6} \mathrm{~m}$, and Earth "B.H" radius $r_{s}=8.75 \times 10^{-3} \mathrm{~m}$, from equation (47):

$$
\begin{aligned}
& g=\frac{r_{s} \cdot C^{2}}{2 \cdot r_{d}^{2}}=\frac{\left(8.75 \times 10^{-3}\right) \cdot\left(3 \times 10^{8}\right)^{2}}{2 .\left(6.36 \times 10^{6}\right)^{2}} \\
& g=9.734 \mathrm{~ms}^{-2}
\end{aligned}
$$

## 15. Conclusion

I concluded that "B.H." energy is the connecting ring between the astronomical and microscopic bodies' attraction by the concept of "Attractive Mass," where the gravity of any body depends on how much mass is being compressed by its "B.H." and not just the amount of mass in that body. In addition, Newton's law of gravity already includes the "Attractive Mass" in the mass of the astronomical bodies it employs; this means that the planet's mass is not a normal mass, but a "Attractive Mass." When calculating gravity on a microscopic scale, the concept of this mass must be taken into account. In addition, I came to the conclusion that the Planck and Fine structure constants are essential for comprehendingthe energy types.

## 16. Data availability

The supporting data for this article can be found in the article itself and in the list of references.

## Statements and Declarations

Conflicts of Interest: The author declares there are no competing interests in this work.

## References

1. Einstein, A. (1916). The foundation of the general theory of relativity. Annalen Phys, 49(7), 769-822.
2. Young, H. A., Freedman, R. D. (2012). Physics with modern physics ,sears and zemansky's university (13th ed.), 757.
3. NIST (National Institute of Stander and Technologt). (2018). Codata Value: Elementary Charge).
4. NIST (National Institute of Stander and Technologt). (2018). Codata Value: Vacuum Electric Permittivity.
5. NIST (National Institute of Stander And Technologt). (2018). Codata Value: Proton Mass.
6. NIST (National Institute of Stander and Technologt). (2018). Codata Value: Newtonian Constant of Gravitation.
7. BIPM (Bureau International Des Poids Et Mesures). (1983). Resolution 1 of the 17th CGPM.
8. Günther, H., Müller, V. (2019). The special theory of relativity, 97-105.
9. L.N. BONDARENKO(KURCHATOV, INST., MOSCOW) V.V KURGUZOV(KURCHATOV, INST., MOSCOW) YU.A. PROKOFEV(KURCHATOV, INST., MOSCOW) E.V. ROGOV(KURCHATOV INST., MOSCOW)P.E. SPIVAK(KURCHATOV INST.,MOSCOW), 328-333
(1978).
10. Young, H. A., Freedman, R. D. (2012). Physics with Modern Physic, Sears and Zemansky's University (13th ed.), 729.
11. NIST (National Institute of Stander and Technologt). (2018). Codata Value: Planck Constant.
12. NIST (National Institute of Stander and Technologt). (2018). Codata Value: Fine-Structure Constant.
13. LIEW, S. C. (2001). Electromagnetic Waves, Centre for Remote Imaging, Sensing And Processing.
14. Mamajek, E. E., Prsa, A., Torres, G., Harmanec, P., Asplund, M., Bennett, P. D., ... \& Stewart, S. G. (2015). IAU 2015 resolution B3 on recommended nominal conversion constants for selected solar and planetary properties. arXiv preprint arXiv:1510.07674.
15. Kutner, M. L. (2003). Astronomy: A physical perspective. cambridge university press.

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