Planetary Emittance And Feedback Parameters Through Varying Climates In Basic Modelling

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Abstract
In search for reproducibility of the results from sophisticated scientific research, the present work focuses on the planetary (longwave) emittance variabilities. A simple model appears applicable through the entire range from very cold to extremely warm climates and for different climate driving forces, i.e. solar luminosity variation and CO_2 concentration change. The results interrelate effects from lapse rate, water vapor, CO_2, and clouds for equilibrium climate states. Feedback parameters are analysed for the emittance decomposition into the atmospheric window, clouds, and the cloud-free atmosphere. A view is devoted to the faint young Sun problem.

Keywords: Climate Modelling; Planetary Emittance; Faint Young Sun Paradox

Introduction

Just as the Sun warms Earth, Earth is cooled by longwave radiation escaping into space. This planetary emittance is strongly interrelated with the vertical temperature profile of the atmosphere which in turn is a result of rather complex balancing mechanisms. Big progress has been achieved incorporating the natural complexity into simulation programs – at the disadvantage that specific understanding is difficult to be extracted. On the other hand, theoretical framework of lower complexity can be too coarse for certain depths of comprehension.

In search for reproducibility of the sophisticated research results, the present studies attempt to sort the importance of phenomena such as: feedbacks from water vapor, lapse rate, and clouds; change of emittance altitude and temperature with surface temperature; cooling of the stratosphere. So far, these topics appear scarcely described in their relation to a general understanding of the natural climate variabilities.

For an assessment by simple means, the present studies make use of observational results where bottom-up computation appears too complex, and combine these with few fundamental principles.

CO_2 Contribution To The Atmospheric Longwave Emittance

Throughout the present work, total planetary emittance is regarded composed of radiation from the surface through the atmospheric window, radiation from clouds, and radiation from the (cloud-free) atmosphere.

From measurements as of Figure 1, planetary emittance from the CO_2 absorption band at wavenumber 670 cm^{-1} (wavelength 15 μm) corresponds to a blackbody temperature of about 217 K, i.e. 6 W/m^2/μm according to the Planck function, the emittance width revealed as approximately 3 μm [1]. Thus, CO_2 radiates into space in the order of 18 W/m^2 – nearly independent of the surface temperature from comparison of the three climate cases in Figure 1. This compares to 169 W/m^2 of total planetary emittance from the atmosphere, i.e. 10 % as rule-of-thumb [2]. The other 90 % of planetary emittance are understood as dominated by water vapor.

It is a simple, but certainly significant observation that CO_2 contributes with 10 % to Earth's cooling and H_2O at nearly 9 times, and that the emittance from CO_2 is almost independent of the surface temperature.
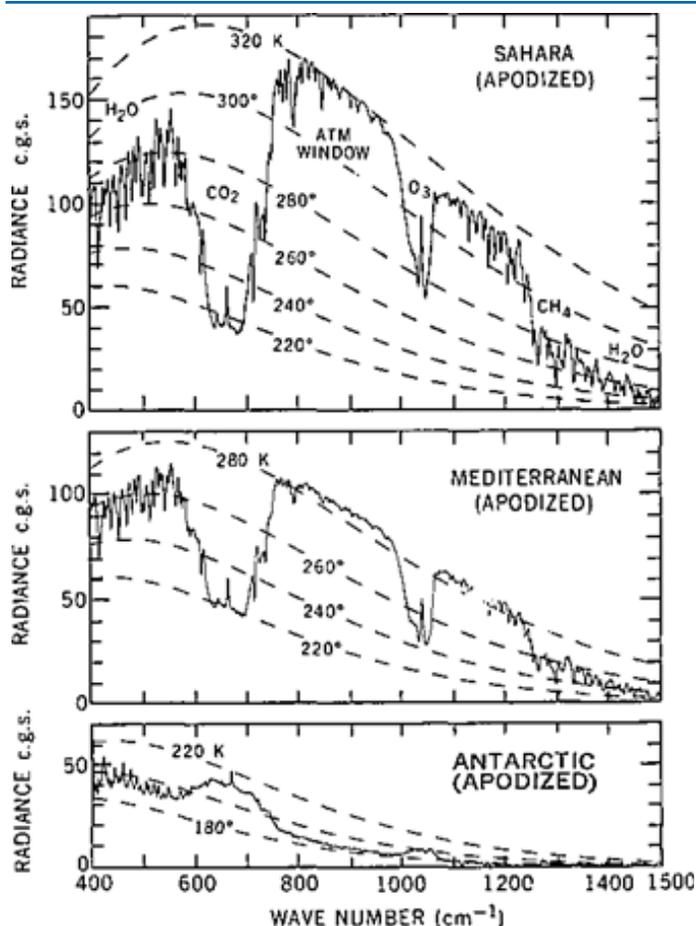
Figure 1: Infrared emittance spectra for three cases, from top to bottom: hot desert, intermediate surface temperature over water, and extremely cold surface condition; blackbody radiances at several temperatures superimposed; from [1].

Three-Component Planetary Emittance And Feedback Parameters
As mentioned, total planetary emittance is regarded composed of radiation from the surface through the atmospheric window, radiation from clouds, and radiation from the (cloud-free) atmosphere. For a first-order estimate, radiation through the atmospheric window is approximated to proportionally scale with the blackbody surface radiation. The present value is taken as 40 W/m^2 [2]. Thus, the window emittance is estimated to increase by about 0.6 W/m^2/K for a surface temperature rise of 1 K. This is equivalent to a feedback parameter of -0.6 W/m^2/K, the minus sign since the emittance increase represents a cooling contribution counteracting the associated temperature increase. (Throughout the present work, the feedback parameter is used to indicate the variations of longwave emittance to space in dependence on the surface temperature.)

From previous sophisticated research, the net effect of clouds was assessed with a feedback parameter of 0.7 W/m^2/K, recently revised to 0.3 W/m^2/K [3].

Now, the specific case is considered of varying surface temperature upon a CO_2 concentration change and unaltered absorbed insolation. In equilibrium states, as e.g. on average approximately experienced during the Eocene, longwave emittance must remain constant since absorbed energy is unchanged [3]. Hence, the feedback parameter of the total planetary emittance is required to be zero (no emittance change upon surface temperature change). With the above values for emittance through the atmospheric window and from clouds, the feedback parameter for longwave radiation from the (cloud-free) atmosphere is required to be either -0.1 or +0.3 W/m2/°C for the two cloud feedback values, respectively. This stimulates a deeper look.

Planetary Emittance In A Simple Model
With this aim, a simplified model has been applied to estimate the longwave emittance from the atmosphere.

Model Description
A summary of the model is depicted in Figure 2. The atmosphere is divided into 1 km-altitude steps. Starting point is an observation-based vertical temperature profile, changing with surface temperature according to the blue lines in Figure 2 (shown for two extreme temperature cases). The stratospheric temperature can be adjusted manually. The lapse rate is 6.5 K/km at 287 K (global annual mean) surface temperature and variable with surface temperature, the studies covering 0 to 0.08 (K/km)/K.

The relative particle densities are given by their mixing ratios multiplied with the general density gradient, the latter to reflect 1/e-diminution per 8 km height. The CO_2 mixing ratio is set constant at all altitudes (dotted green line in Figure 2). The H_2O mixing ratio (i) follows the vertical pattern as depicted in Figure 2 (dashed orange line), (ii) is temperature dependent at the ground, 0.4 volume-% for 288 K – temperature dependency either linear by 9.2 %/K (approximation for the longwave revealed in absorption-to-temperature relationship), or exponential by 7 %/K (close to the Clausius–Clapeyron relation), or proportional to the saturation water vapor pressure (Tetens equation); (iii) the vertical densities are scaled proportionally to the ground value .

Radiation occurs according to the blackbody at any location in the atmosphere and is proportional to the wavelength-related absorbing/emitting particle densities. The spectrum is divided into three regimes: one for the CO_2 absorption band at 15 µm and two for the adjacent wavelengths, represented by 7 and 21 µm, in the model solely related to H_2O. The wavelength regimes are treated separately. The wavelength span for each regime is determined to match the reported 169 W/m^2 of emittance at 289 K; in result, the wavelength spans are 3 µm for the 15 µm-CO_2-regime, 11.7 and 9 µm for the regimes at 7 and 21 µm, respectively [2]. To avoid a radiation bias dependent on surface temperature with the effect to synchronize model surface radiation with the (ideal) blackbody radiance, the wavelength spans vary with surface temperature by -0.009 and 0.005 µm/K for 7 and 21 µm, respectively.

For the transmissivity to space from a certain altitude, the attenuation of upward radiation is taken as inverse-exponential to the

aggregated particle densities above the considered altitude divided by a density length. The latter is determined such that the spectral emittance matches the measurements of Figure 1: as mentioned earlier for CO_2, the average emittance corresponds to an effective temperature of about 217 K, thus to 6 W/m²/μm for 15 μm wavelength; for 'H_2O', the measurement for the Mediterranean climate is taken as reference, the average effective emittance temperature read from Figure 1 as 257 K, thus with 7.6 W/m²/μm for 7 μm wavelength and 6.9 W/m²/μm for 21 μm. From this, the density lengths are $7 \cdot 10^{-5}$ for CO_2 and $2 \cdot 10^{-4}$ for the 'H_2O' wavelengths. These values are assumed relating to a surface temperature of 288 K.

Hence, Planck's spectral exitance (here denoted as Bz,λ, with the dependencies on altitude, z, and wavelength, λ) together with the vertical profiles of particle density and temperature determine the vertical transmittance distribution. Transmittance to space from a specific altitude is reflected into the prescribed temperature at the next higher altitude interval, effective relative to pre-industrial conditions. The atmospheric emittance to space is the sum of the transmittances from all altitude intervals and all wavelengths.
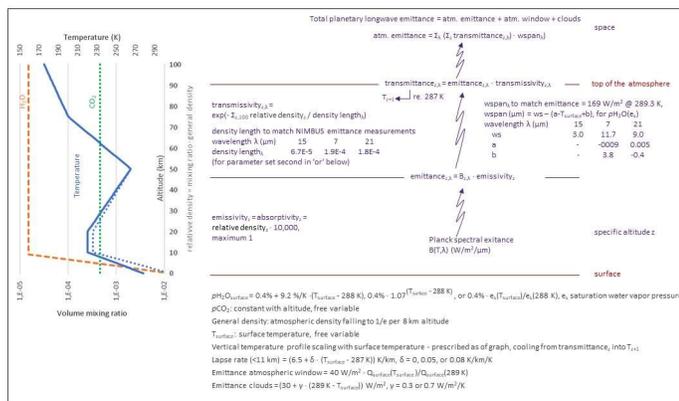

Figure 2: Depiction of the estimation scheme for atmospheric emittance to space via the vertical transmittance distribution, the longwave spectrum represented by the CO_2 absorption band at 15 μm and the adjacent H_2O-dominated absorption regimes at 7 and 21 μm; graph insert showing the vertical patterns of temperature and volume mixing ratios for water vapor and CO_2 at reference conditions related to 288 K surface temperature.

Total planetary longwave emittance is the sum of the emittances from the atmosphere (modelled as described), through the atmospheric window (approximated as described earlier), and from clouds. For the atmospheric window, a closer inspection has revealed that the chosen approximation is applicable for the studied conditions (details not presented). The emittance from clouds is scaled proportionally to the surface temperature by the feedback

parameter, see the following notes on the considered values, with reference emittance of 30 W/m2 at 289 K [2].

The estimation scheme certainly represents a strong simplification of nature's complexity. Sensitivity studies have been performed by varying the temperature dependencies of H_2O density and lapse rate as well as the feedback parameter for the net emittance effect from clouds. Furthermore, the analysis has covered a wide range of climate situations including extremes such as 278 K and 315 K of surface temperature. Two climate driving forces have been considered: CO_2 or insolation determining the temperature variabilities, albedo changes from snow/ice taken into account at the lower temperatures. The subsequent presentation concentrates on the results revealed as robust, with the specific parameter base: scaling of the H2O concentration-temperature dependency by the saturation water vapor pressure, 0.05 (K/km)/K lapse rate temperature dependency, and 0.7 W/m²/K cloud feedback. The latter agrees well with the 0.8 W/m²/K inferred from the comparison between all-sky energy budget studies and clear-sky measurements [2]. The considered albedo effects are, relative to 287 K surface temperature (minus/plus for cooling/warming effect): -14, -3, +1, +2 W/m² for 278, 284, 291, >294 K, respectively.

Model Results
CO_2 Driving Temperature
For the case of CO_2 driving temperature, the observed CO_2-temperature situations of the Eocene are well reproduced by the simple model, also when extrapolated to 284 and 306 K, corresponding to atmospheric CO_2 concentrations between 176 and 3600 ppmv (see Table 1 for details) [4]. Condition is that the stratospheric temperature is reduced relative to the prescribed profile between about 291 K and 300 K surface temperature, the reduction topping at -29 K. The pattern of the stratospheric cooling is expected to arise from CO_2 radiation to space and ozone temperature dependencies.

Emittance altitude and temperature are found to change with surface temperature. For instance for the surface temperature rise from 284 to 306 K, with the CO_2 concentration rising from 176 to 3600 ppmv, peak emittance altitudes and temperatures increase in the order of 1.5 km and 10 K for the 'H_2O' wavelengths and by 25 km and 20 K for CO_2, respectively.

From pre-industrial conditions (287 K surface temperature, 276 ppmv CO_2) to very hot climates (306 K, 3600 ppmv), the atmospheric emittance varies in non-linear manner with surface temperature. For the regime of CO_2-doubling from pre-industrial, the (clear-sky) atmosphere emittance increases by 0.36 W/m²/K, corresponding to the feedback parameter of -0.36 W/m²/K.

Table 1: Planetary emittance for various climates, CO_2 concentration driving temperature. Input values: surface temperature $T_{surface}$ with corresponding surface blackbody radiation $Q_{surface}$; atmospheric CO_2 volume mixing ratio pCO_2, related to $T_{surface}$ according to the Eocene CO_2-temperature relationship [4]; changes of absorbed insolation from glaciation-related albedo relative to implicit reference climate; stratospheric temperature relative to the present. Model results, columns 4-6: emittance from the (cloud-free) atmosphere, from clouds and through the atmospheric window.

pCO_2 driving surface temperature								
$T_{surface}$ (K)	$Q_{surface}$ (W/m²)	pCO_2 (ppmv)	Emittance (W/m²)				Absorbed insolation change (W/m²)	Stratospheric temperature change (K)
			atmosphere	clouds	atm. window	glaciation	insolation	
284	368.9	176	168.2	33.5	37.3	-2.1	-	0
287	384.7	276	171.8	31.4	38.9	1	-	0
291	406.6	500	173.5	28.6	41.1	2	-	0
291.7	410.5	552	173.4	28.1	41.5	2	-	- 3.5
296	435.3	1050	175.2	25.1	44.0	3	-	-22
297	441.2	1225	175.3	24.4	44.6	3	-	-29
306	497.1	3600	175.7	18.1	50.3	3	-	-18

Temperature Driving CO_2

For the case of absorbed insolation driving temperature, the CO_2 concentration roughly follows surface temperature by 20 ppmv/K [4]. At low temperatures, the present consideration views albedo changes as climate driver. At higher temperature with vanished glaciation, solar luminosity variation is taken as the dominant climate driver. In these cases for equilibrium states, longwave emittance must increase in line with absorbed energy.

In result, the simple model can well reflect the conditions from 278 to 315 K if the stratosphere warms with solar luminosity rise (see Table 2 for details). The warming is interpreted to originate from larger shortwave absorption as insolation increases.

The feedback parameters are revealed rather independent of the surface temperature above 284 K, here listed together with insolation forcing per temperature change: +1, +0.7, -0.6, -1.1 W/m2/K for absorbed insolation, clouds, atmospheric window, atmosphere.

Table 2: Planetary emittance analogous to Table 1, here temperature driving atmospheric CO_2 concentration. Differences to Table 1: atmospheric CO_2 mixing ratio pCO_2 proportional to surface temperature with 20 ppmv/K; changes of absorbed insolation from glaciation or insolation change relative to pre-industrial [4].

pCO_2 driving surface temperature								
$T_{surface}$ (K)	$Q_{surface}$ (W/m²)	pCO_2 (ppmv)	Emittance (W/m²)				Absorbed insolation change (W/m²)	Stratospheric temperature change (K)
			atmosphere	clouds	atm. window	glaciation	insolation	
278	338.7	100	156.4	37.7	34.2	-13	0	0
284	368.9	220	168.7	33.5	37.3	-1.7	0	0
287	384.7	280	171.8	31.4	38.9	1	0	0
295	429.4	440	179.5	25.8	43.4	3	5	10
305	490.7	640	190.2	18.8	49.6	3	15	30
315	558.2	840	200.0	11.8	56.5	3	25	31

Dealing With Cloud Feedback Uncertainties

The present model appears applicable for the entire range of cloud feedback parameters reported from the sophisticated simulations (i.e. 0.7 and 0.3 W/m²/K, see above) when adapting the stratospheric temperature. Cloud feedback is considered as fit parameter in the present approach. The results appear soundest if the longwave radiation from clouds varies with surface temperature by 0.7 W/m²/K (for preciseness, representing the compound effect related to clouds).

Atmospheric CO_2 Concentration Doubling

Using the Eocene as blueprint for doubling of the atmospheric CO_2 concentration, equilibrium is given at 287 K surface temperature for 276 ppmv CO_2 concentration and at 291.7 K for 552 ppmv [4].

For the transition to the double-CO_2 target state, the present scheme yields a feedback parameter for the atmospheric emittance of -0.36 W/m²/K (see above), dominated by CO_2 (80 %) with near-cancellation between the 'H$_2$O' wavelengths. The other feedback param-

eters are estimated to: absorbed insolation (from snow/ice albedo) +0.21, clouds +0.7, and atmospheric window -0.55 W/m²/K.

Earth During the Faint young Sun

Since a tool has come at hand to even look at very high temperatures and CO_2 concentrations, it seems interesting to have a view on the faint young Sun problem, related to the period from the Early Archean to the Late Proterozoic, 4 to 1 Ga before present (BP). The period is characterized by relatively low Sun luminosity, high Earth temperature, high atmospheric CO_2 and low oxygen concentration, and the transition from mostly oceanic coverage to nearly the present continental emergence. Insolation at the top of the atmosphere was approximately 80 and 20 W/m² below the current level at 4 and 1 Ga BP, respectively [4]. Temperature and atmospheric composition are only known with high uncertainties. For the present analysis, the regarded values have exemplary character: A surface temperature of 306 K with atmospheric CO_2 concentrations of 30,000 and 3,600 ppmv at 4 and 1 Ga BP, respectively.

It is expected that the low atmospheric oxygen concentration has caused a stratospheric cooling contribution due to reduced short-wave absorption. On the other hand, lower atmospheric shortwave absorption has entailed higher shortwave fraction being absorbed at the ground. In the present estimates, shortwave absorption in the atmosphere is first scaled from pre-industrial via the top-of-the atmosphere insolation and in addition, the low-oxygen effect is approximated by a reduction (of the atmospheric shortwave absorption) by 10 and 5 W/m² for 4 and 1 Ga BP, respectively. The stratospheric temperature is assumed lower than contemporarily in the order of 100 and 59 K for the two times.

As result, the simple model of the present studies can well reflect the faint young Sun times, in accordance with energy budget considerations (see Table 3 for details), if the planetary albedo was 0.13 in the Early Archean (4 Ba BP). At first sight, this appears far from reasonable. To examine this: As mentioned, the Early Archean exhibited high temperatures and near-complete oceanic coverage. Thus, the present tropic oceans may give guidance. Figure 3 shows measurement results for the present planetary albedo. For tropic oceans, 0.13 seem in the vicinity of the observed values.

Table 3: Key figures for planetary emittance estimates related to the Early Archean and Late Proterozoic with pre-industrial conditions as reference; SW for shortwave, LW for longwave, TOA for top of the atmosphere, pCO_2 for atmospheric CO_2 volume mixing ratio. Upper section: characteristic conditions [2]. Middle section: estimates from the energy budget; lower section: estimates from the present simple model

	Early Archean	Late Proterozoic	pre-industrial
Time (Ga BP)	4	1	0
GENERAL CONDITIONS			
Insolation (SW) TOA (W/m²)	261	321	341
re. pre-industrial	-80	-20	-
Temperature (K)			
surface	306	306	287
stratosphere re. pre-industrial	-100	-59	-
pCO_2 (ppmv)	30,000	3,600	276
factor re. pre-industrial	107	13	
Low-oxygen effect (W/m²)			
shortwave absorption stratosphere	-10	-5	-
Continental coverage			
continent, plus ice	0.027, 0	-	0.265, 0.03
ocean, plus ice	0.973, 0	-	0.685, 0.02
Temperature and continental coverage effect			
planetary albedo	0.13	0.27	0.3
ENERGY BUDGET			
SW reflection from albedo (W/m²)	34	86	102
SW after albedo (absorbed insolation) (W/m²)	227	235	239
Absorbed insolation re. pre-industrial (W/m²)	-12	-4	-

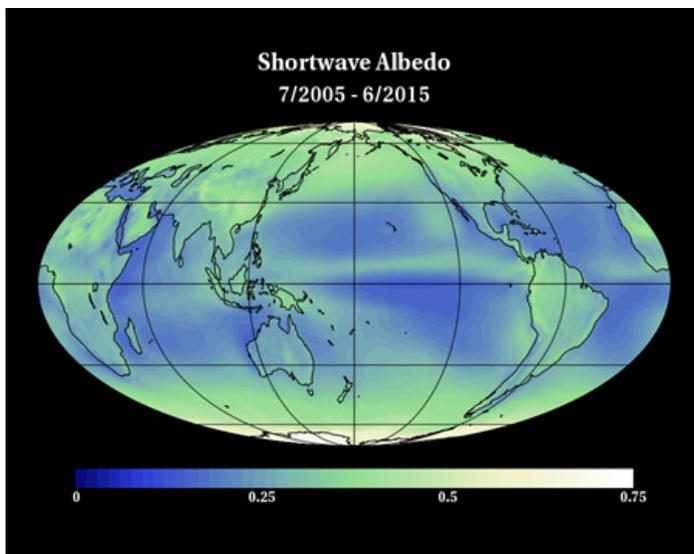|			
LW atmosphere to surface (W/m²)	424	434.5	333
LW planetary emittance (W/m²)	227	235	239
of this clouds	18	21	30
clear sky	159	164	169
atmospheric window	50	50	40
Planetary emissivity	0.457	0.473	0.602
EMITTANCE - PRESENT MODEL			
LW planetary emittance (W/m²)	227	235	242
of this clouds	18	18	31
clear sky	159	167	172
atmospheric window	50	50	39
difference to energy budget	0	0	3

Figure 3: Measured annual top-of-the-atmosphere shortwave albedo; image courtesy of the CERES Science Team at NASA Langley Research Center in Hampton, Virginia, USA [5].

In conclusion, it would come with no surprise if the faint young Sun problem were called resolved from sophisticated studies.

Discussion

It has been perceived challenging to extract the essentials on nature's processes from sophisticated research and to identify the topics relevant for the broader public. Also partly, there has been a missing link between qualitative explanations and quantitative reproducibility. The general idea is that such gaps may be filled by identifying the driving forces with help of simple models.

The present studies have focused on the planetary emittance as one of the fundamental regulators of Earth's climate. The inherent complexity of the underlying intertwined processes is reduced, first by decoupling planetary emittance from the longwave absorption in the low troposphere. Second, the emittance subdivision is chosen as radiation from clouds, from the (cloud-free) atmosphere, and through the atmospheric window. Third, observed information is used as input where bottom-up computation is too complex for simple modelling. Fourth, only few basic principles are applied.

The resulting simple model can well describe a wide range of climate situations, including doubling of the CO_2 concentration and the faint young Sun; key criterion is that energy balance be established at all considered climate states. This model success is regarded as confirmation that the driving forces are correctly identified, particularly the water vapor- and lapse rate - temperature dependencies as well as the stratospheric temperature variations. The model setup is interpreted to well reflect on average the interplay of the diverse underlying processes.

The results on the natural variabilities in brief: Emittance altitude and temperature increase in line with surface temperature. – Lapse rate is an intrinsic feature closely tied to the surface temperature, hence not assigned to a separate role in planetary emittance. A surface temperature dependency of 0.05 (K/km)/K appears as a realistic mean value. – In contrast, water vapor has an active role. The emittance from the 'H_2O' wavelengths in absolute terms, i.e. nearly 90 % of atmospheric emittance, reveals strong sensibility to details of the tropospheric temperature profile. – The stratospheric temperature is inferred to exhibit vital adaptation at surface temperatures above 291 K. – Emittance from CO_2 is strongly influenced by stratospheric temperature variabilities. – The present model principally works for a range of cloud feedback parameters; 0.7 W/m²/K is the preferred value in view of the sound results and the consistency with energy budget comparisons (based on accounting scheme as well as measurements). – For equilibrium upon CO_2 concentration doubling from pre-industrial, the total feedback parameter is constrained by the contributions from the atmospheric window, the clouds, and albedo; radiation from the atmosphere delivers -0.36 W/m²/K, revealed as CO_2-dominated with 80 % (in relative terms between the two variability cases). – The present approach may point towards an explanation of the faint young Sun climates.

The hope is that provision of a simple model such as the present helps to filter the essential and to offer reproducibility and transparency.

Supplementary Materials:
All data and code are available: https://www.dropbox.com/scl/fi/k26kfmb8n2n6qwy3rv0wm/Planetary-emittance-and-feedback-parameters-data-and-code.xlsx?dl=0&rlkey=xzvgt6tthwa2e09pzod89cokq

Conflicts of Interest:
No conflict of interest is to be declared.

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