

## Fermat's Theorem Arithmetic Demonstration

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### Abstract

One of the factors of the number  $A+B-C$  is a fraction proper.

### Theorem

In a prime base  $n > 2$  and reciprocals prime (coprime) numbers  $A, B, C$ , not multiples of  $n$  (basic case), the equality

- $A^n + B^n - C^n = 0$  impossible.

### Simplest Properties of Fermat's equality (1) In the Basic Case

- $A+B=c^n, C-B=a^n, C-A=b^n$ . And  $a^n + b^n = (a+b)r^n, c^n - b^n = (c-b)p^n; c^n - a^n = (c-a)q^n$ .
- $A = ap, B = bq, C = cr$ ; where the numbers  $a, b, c, p, q, r$  [like numbers in pairs  $a+b$  and  $r^n$ ;  $c-b$  and  $p^n$ ;  $c-a$  and  $q^n$ ] are reciprocals prime.
- $U = A + B - C = ap - a^n = bq - b^n = c^n - cr = (c^n - a^n - b^n)/2 = abc$  (where, how easy it is to see, numbers  $v (=abc)$  and  $u$  are reciprocals prime).
- $a', b', c'$  – greatest common measures (G.C.M.) in pairs  $(a, c-b), (b, c-a), (c, a+b)$ .  $U'$  is number  $a'+b'-c'$ .  $p', q', r'$  are numbers  $(c^m - b'^m)/(c' - b')$ ,  $(c^m - a'^m)/(c' - a')$ ,  $(a'^m + b'^m)/(a' + b')$ .  $c' > 1$ .

### Proof of the Theorem

If  $U' = 0$ , then  $c'^2 - a'^2 - b'^2 = 2a'b'$  with the fraction proper  $(2a'b')/(2a'b'c')$  (see 4)!

And after the recovery of all the factors of the number  $U$ , the fraction  $1/c'$  remains.

And if  $U' \neq 0$ , then with the recovery of the number  $U$  the term  $c'$  multiplies by  $c'^{m-1}$ , and the term  $a'+b'$  multiplies by  $r'$  (see 5), which is reciprocals prime (coprime) numbers with the denominator  $a'b'c'$ . Consequently, the fraction  $(a'+b'-c')/(2a'b'c')$  of the number  $U$  remains, and the Fermat's equality (1) in integers is impossible.

The theorem is proven.

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