

Comparative Study of Decentralized Grid-Forming Converter Controls for Inverter-Based Microgrids

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Submitted: 2025, Aug 04; **Accepted:** 2025, Sep 08; **Published:** 2025, Sep 11

Citation: Kelada, F., Buire, J., Hadjsaid, N. (2025). Comparative Study of Decentralized Grid-Forming Converter Controls for Inverter-Based Microgrids. *Arch Cienc Investig*, 1(2), 01-06.

Abstract

With the heavy integration of Inverter-based Resources (IBR) into the different levels of the electrical network, they are gradually requested to replace the conventional Synchronous Machines (SM) in maintaining the network voltage and frequency references. Such Grid-forming (GFM) controllers recently reported in literature include conventional Droop control, nonlinear oscillator-based controls, namely the dispatchable Virtual Oscillator Control (dVOC), Synchroverter and Matching controls. This article aims to reveal the underlying resemblance between these grid-forming controls and the conventional Droopbased strategies being the most commonly used in the decentralized and hierarchical control of Microgrids (MGs). Based on the derived similarities in their dynamics, tuning the different controllers' parameters to achieve equivalent transient and steady state dynamics maintaining P-f and Q-V relations is deduced and validated using time domain simulations.

Keywords: Decentralized Control, Grid-forming Converter Controls, Inverter-Dominated Networks, Microgrids, Tuning of Grid-Forming Power Controllers

1. Introduction

Stability and resilience of the electrical power networks is the uttermost priority of the network operators. These cornerstone characteristics of the power systems have been maintained all over the years by huge generation plants that were traditionally dominated by Synchronous Machines (SM) of gigantic inertia reservoir and well-established electromechanical interactions maintaining the synchronization and stiffness of the network. Lately with the gradual retraction of SMs, power converters interfacing IBRs are slowly taking over the role of maintaining this synchronization and stiffness of the network by forming themselves the voltage magnitude and frequency references [1].

In that sense, many grid-forming control strategies are being reported in literature. Droop-based primary control—and its variants—is the most commonly used grid-forming control in networks with parallel operation of inverters such as MGs. This is due to many obvious reasons, such as ease of implementation, resemblance to conventional SMs' primary control and decentralized power sharing capabilities [2-5]. The recent research on grid-forming controls for voltage source converters presents other novel strategies to control the converters in a grid-forming manner as explained above [6,7]. A wide range of such inverter controls proposed in literature are called the Virtual Synchronous

Generator (VSG).

These controllers emulate some of the SMs' dynamics to generate the control signals for the converters [1,7]. Others match the converters' dynamics to that of SMs and prove that the DC-link capacitor voltage dynamics are analogous to the rotational speed in SMs and thus can be utilized to mimic SMs' synchronization with the grid in what is called the Matching control [8]. Others relied on modelling converters as coupled oscillators and define a control law to synchronize such oscillators using consensus-like dynamics as with the case of Virtual Oscillator Control (VOC) and its dispatchable variant the (dVOC) [9].

The vast majority of these grid-forming controllers deduce the frequency information from the active power imbalance and similarly with the voltage reference signal using knowledge of the reactive power change to maintain parallel loadsharing with other parallel units. In this article, a comparative analysis of these P-f and Q-V dynamics in the previously mentioned GFM controls is carried out and resemblance to the conventional droop functions are highlighted. The contribution of this paper is thus twofold, first by putting the P-f and QV dynamics of the different GFM controllers in the same canonical form, their steady state and

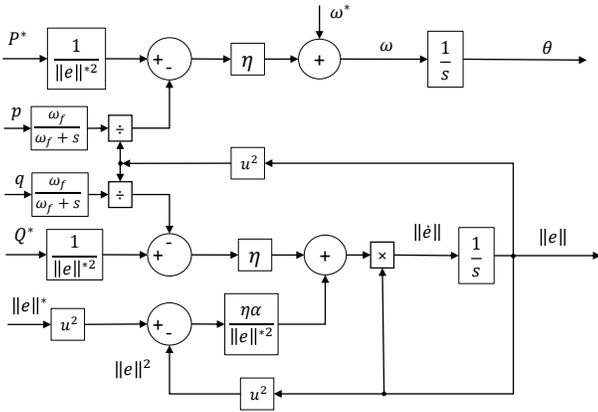


Figure 4: dVOC Controller

2.4 Matching Control

Another analogous control to VSG, is the matching control, which is designed to assure that the closed-loop dynamics of the converter exactly match that of SMs, in the sense that the DC-link capacitor voltage serves as the key control and imbalance signal in a similar fashion as is SM's rotational speed is an indication of equilibrium between generation and consumption. The objective of this control is thus to mimic the SG's synchronization with the grid through mimicking its electromechanical interactions [8,15].

In order to incorporate these dynamics in the control, the angle dynamics of the matching control can be obtained by dynamic feedback of the measured DC voltage as shown in (10) [8], or expressed in relative coordinates as in (11) [7].

$$\omega = \gamma \cdot v_{dc} \quad (10)$$

$$\omega - \omega_0 = K_\theta (v_{dc} - v_{dc}^*) \quad (11)$$

where the constant $\gamma = \omega_f / v_{dc}^* > 0$ encodes the ratio between the

nominal AC frequency ω_0 and the DC reference voltage v_{dc}^* and $K_\theta > 0$ is a gain to be tuned.

Assuming a P-controller to control the DC-link capacitor voltage (cf. Figure 1) such that:

$$i_{dc} - i_{dc}^* = K_{p,dc} \cdot (v_{dc}^* - v_{dc}) \quad (12)$$

Substituting by (12) in (11) and exchanging i_{dc} by p/v_{dc} and i_{dc}^* by P^*/v_{dc}^* we get:

$$\omega - \omega_0 = \frac{K_\theta}{K_{p,dc} \cdot v_{dc}^*} (P^* - p) \quad (13)$$

Finally, considering the low-pass filter effect (cf. Fig. 5), we can express the matching control dynamics in time domain as:

$$\frac{v_{dc}^* K_{p,dc}}{\omega_f K_\theta} \frac{d\delta\omega}{dt} = P^* - p - \frac{v_{dc}^* K_{p,dc}}{K_\theta} \cdot \delta\omega \quad (14)$$

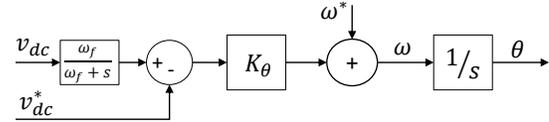


Figure 5: Matching Controller

3. Uncovering the Underlying Dynamics

The information on how each controller deduces the rotational electrical frequency (ω) from the change in active power can be concluded from (1), (3), (8) and (14) and is summarized in Table I to highlight the equivalences in dynamics. Similarly, the information on how each controller computes the reference voltage magnitude for the inner control loops from the reactive power imbalance information can be deduced from (2), (4) and (9) and summarized in Table I.

P-f Dynamics					Q-V Dynamics				
	Transient Term			S.S. Term	Transient Term			S.S. Term	
Droop	$\frac{1}{m_p \omega_f}$	$\frac{d\delta\omega}{dt} =$	$P^* - p$	$-\frac{1}{m_p} \delta\omega$	$\frac{1}{n_q \omega_f}$	$\frac{d\delta E}{dt} =$	$Q^* - q$	$-\frac{1}{n_q} \delta E$	
VSM	$J \omega^*$	$\frac{d\omega}{dt} =$	$P^* - p$	$-D_p \omega^* \delta\omega$	K	$\frac{d\varphi}{dt} =$	$Q^* - q$	$-D_q \delta E$	
dVOC	$\frac{\ e\ ^{*2}}{\eta \omega_f}$	$\frac{d\delta\omega}{dt} =$	$P^* - p$	$-\frac{\ e\ ^{*2}}{\eta} \delta\omega$	$\frac{2\alpha \ e\ ^{*2}}{\omega_f}$	$\frac{d\delta E}{dt} =$	$Q^* - q$	$-\frac{\ e\ ^{*2}}{\eta} \delta E$	
Match.	$\frac{v_{dc}^* K_{p,dc}}{\omega_f K_\theta}$	$\frac{d\delta\omega}{dt} =$	$P^* - p$	$-\frac{v_{dc}^* K_{p,dc}}{K_\theta} \delta\omega$					

Table 1: Summary

Comparing these P-f dynamics with the well-known SMs'swing equation shown in (15), we can deduce by identification the terms incorporating the controllers' tuning parameters relative to the inertia constant (H), which in other words, define mathematically how the frequency signal's rate of change will be in case there is an imbalance in the active power. We can also deduce the terms relative to the frictional damping (D) which in this context represents the steady state error in the frequency signal from the primary control.

$$2H \frac{d\delta\omega}{dt} = P_m - P_e - D \cdot \delta\omega \quad (15)$$

It is clear how the choice of the measurements' filter cut-off frequency ω_f affects the transient rate of change of the frequency. Lower values of the cut-off frequency is usually required to achieve good attenuation of high frequency distortion components in the measured quantities and avoid any interactions with inner control loops [11]. This will directly solve the issue with the synchroverter's outer voltage regulation time constant τ_v , also since $\tau_v \approx 1/\omega_f$.

By choosing the suitable filter cut-off frequency and since the droop coefficients are easy to set from relations (16), one can tune by identification all the other controllers' parameters as summarized in the upper third of Table II. This tuning criteria thus sets the required transient and steady state behavior of the frequency and voltage output signals by tuning the transient and steady state terms as marked in Table I.

$$m_p = \frac{\Delta\omega}{\Delta P}, \quad n_q = \frac{\Delta V}{\Delta Q} \quad (16)$$

To test and validate the previous claims, the four controllers compared in this paper are implemented in the upper power controller modules of a classic cascaded controlled voltage source converter as previously mentioned. The test network consists of two 10 kVA, 400V (RMS phase-to-phase) VSC converters each connected in parallel through a line to a 10 kW (pure resistive) constant impedance load ($\equiv 14.52\Omega$ per phase) as shown in Figure 1. A load step increase of +0.33 p.u is simulated at $t=1.5s$ and decreased back to normal again at $t=2.5s$ to compare the P-f and Q-V dynamics of the different controllers. The equivalent tuning of the different controllers' parameters according to the established criteria and equivalent dynamic equations is shown in Table II.

Controller	Tuning Parameter Equivalent	Controller	Tuning Parameter Equivalent
Droop	$m_p = \Delta\omega / \Delta P$	Matching	$K_\theta = m_p \cdot K_{p,dc} \cdot v_{dc}^*$
	$n_q = \Delta V / \Delta Q$		—
dVOC	$\eta = m_p \cdot \ e\ ^{*2}$	VSM	$D_p = 1/m_p \cdot \omega_b, J = 1/m_p \cdot \omega_b \cdot \omega_f$
	$\alpha = 1/2n_q \ e\ ^{*}$		$D_q = 1/n_q, K = 1/n_q \cdot \omega_f$
Cascaded Current/Voltage Controllers (in p.u)			
$K_{pVL} = 0.4744$	$K_{iVL} = 51$	$K_{pCL} = 0.5394$	$K_{iCL} = 586.9$
Droop Controller			
$m_p = 1.5708 \times 10^{-4}$ (0.5%)	$n_q = 6.667 \times 10^{-5}$ (0.1%)	$\omega_f = 0.05\omega_b$	
Virtual Synchronous Machine (VSM)			
$D_p = 20.264$	$J = 1.2901$	$D_q = 15 \times 10^3$	$K = 954.88$
Dispatchable Virtual Oscillator Control (dVOC)			
$\eta = 25.1327$	$\alpha = 18.75$	$\ e\ ^{*} = 400V$	
Matching Control			
$K_\theta = 0.1885$	$K_{p,dc} = 1.5$	$v_{dc}^* = 800V$	
Lines Parameters			
$R_{l1}/X_{l1} = 2.3$		$R_{l2}/X_{l2} = 0.6$	

Table 2: Network and VSCs' Control Parameters

Figures 6a, 6b show the active power supplied by the first converter and the deduced frequency signal respectively. It could be noticed how the rate of change of frequency (ROCOF) as well as the steady state frequency value is quasi-identical by all the different controllers which validates the previously derived P-f dynamic equations and the respective tuning in steering the P-f dynamics to behave in a controlled and droop-equivalent manner. In a similar fashion, Figures 6c,6d show the reactive power supplied by the same converter and the measured voltage magnitude at the capacitor filter. Again, quasi-identical voltage and reactive power

dynamics are spotted which validates by its turn the aforementioned proposed equivalence of the Q-V dynamics between the different controllers and the validity of the tuning criteria in controlling the Q-V behavior according to user preferences.

This configuration and results were tested in a wide range of the feasible values of the droop coefficients while respecting the same tuning method and again the same conclusions were obtained. On the other hand, choosing other non-equivalent values for the tuning parameter, each controller starts to behave differently

and the quasi-identical dynamics start to deviate. Which further validates the analysis conducted here.

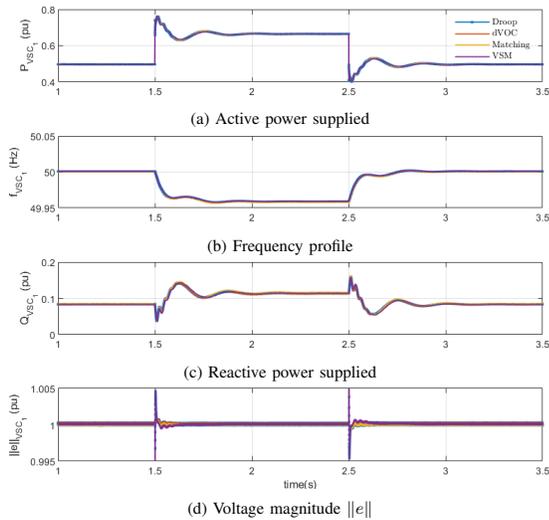


Figure 6: VSC Converter 1 Response to the Load Step at $t=1.5-2.5s$

4. Conclusions

In this article the embedded droop-like dynamics of the four major grid-forming controllers proposed for VSCs in literature, namely the Droop, dVOC, Synchroverter and Matching are compared and the underlying equivalences are highlighted and then utilized to achieve equivalent tuning of the controllers' dynamics to obtain equivalent P-f and Q-V relationships. It could be deduced how—regardless of the different control architecture and different tuning parameters—they can all be reduced to the very similar dynamics and thus by identification their different parameters can be tuned equivalently to the well-known Droop coefficients.

The derived dynamic equations and the resulting tuning method guarantee equivalent parallel active and reactive load power sharing, controlling the rate of change of the deduced frequency and voltage signals and their steady state values as well as being intuitive, easy to implement and representative of the physical meaning of each tunable value of the different controllers. However, the utilization and generalization of this approach in studying the limits of stability of the individual controllers needs further research.

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